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Constrained Type Families

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Two main contributions:

1. Discovering the problem:



GHC assumes all type families are total.

2. First type safety proof with



non-termination and non-linear patterns.

Simpler
metatheory

But first:
An introduction to
type families

In Haskell,
type families

=


type functions

results applicable to any language with
partiality and type-level computation

```
class Collects c where
  type Elem c
  empty    :: c
  insert  :: Elem c → c → c
```

```
instance Collects [a] where
  type Elem [a] = a
  ...
```

equality axiom



```
instance Collects Word where
  type Elem Word = Bool
  ...
```


axiom is independent of class

type family Elem c

class Collects c where

empty :: c

insert :: Elem c → c → c

```
data Z
data S n
```

```
type family Pred n
type instance Pred (S n) = n
type instance Pred Z = Z
```

Haskellers leave no
feature ununused

data Z

data S n

closed type family

type family Pred n where

Pred (S n) = n

Pred n = n



Our new old idea:
Constrained Type Families

(originally suggested by
Chakravarty et al., ICFP '05)

Definitions

A **ground type** has no type families.

A **total type family**, when applied to ground types, always equals some ground type.

Constrained Type Families

- All partial type families are associated
- Class constraint necessary to use an associated type family

Example

```
type family F a
```

```
thwack :: F a → Maybe a
```

```
thwack = ...
```



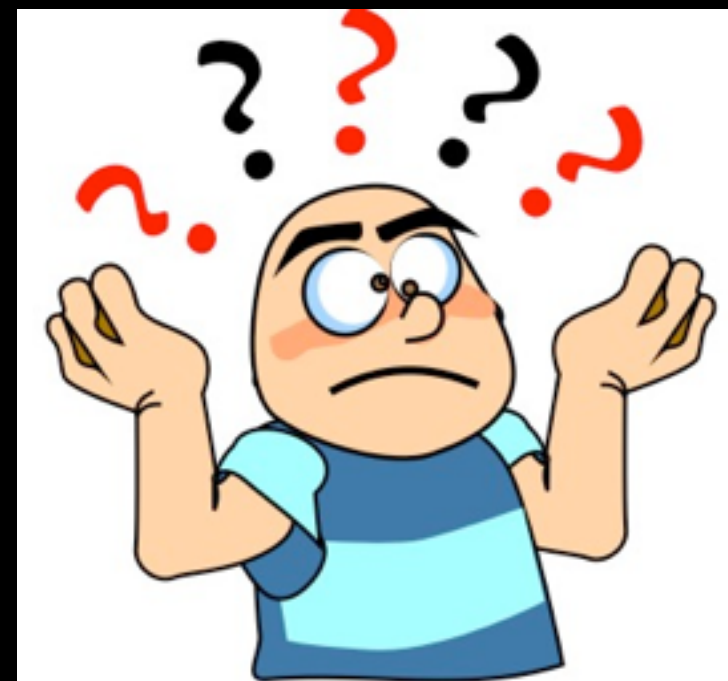
Example

class CF a where
type F a



thwack :: CF a ⇒ F a → Maybe a
thwack = ...

The Totality Trap

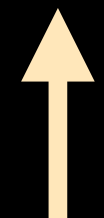


Wat #1

type family F a

x = fst (5, \perp :: F Int)

that's not a type!



Ok, modules loaded: Wat.

Wat #1

```
class CF a where  
  type F a
```



```
x = fst (5, ⊥ :: F Int)
```

↑
that's not a type!

```
error: No instance for (CF Int)
```

Wat #2

```
type family EqT a b where
```

```
  EqT a a = Char
```

```
  EqT a b = Bool
```

This has bitten!

In real life!

```
f :: a → EqT a (Maybe a)
```

```
f _ = False
```

To people who use
Haskell to make \$\$\$!

```
Wat.hs: error: ...
```

Wat #2

```
type family EqT a b where  
  EqT a a = Char  
  EqT a b = Bool
```



```
f :: a → EqT a (Maybe a)  
f _ = False
```

Ok, modules loaded: NoWat.

Why Wat #2?

type family `Maybes a`

type instance `Maybes a =`

`Maybe (Maybes a)`

`f :: a → EqT a (Maybe a)`

with $a \mapsto \text{Maybes Int}$,

$a = \text{Maybe } a!$

Wat #3

```
type family Maybes a
```

```
type instance Maybes a =
```

```
    Maybe (Maybes a)
```

```
justs = Just justs
```

```
Wat.hs: error:
```

- Cannot construct the

infinite type:

$a \sim \text{Maybe } a$

type inference fail.

Red herring:
“Just ban **Maybes!**”

Sometimes we
need loopy type families.

Wat #3

instance CMaybes a \Rightarrow CMaybes a where
type Maybes a = Maybe (Maybes a)

justs = Just justs

Wat.hs: error:

- Cannot construct the infinite type:
a ~ Maybe a

GHC does not infer impossible constraint.



The fundamental problem:

GHC today assumes all
type families are total.

Constrained type families fix this.

Why does this fix the wats?

The class constraint
restricts the type
family domain.



First known proof
of consistency with
non-linear patterns
and
non-termination.

Wrinkle:

Total type families

Total type families need
not be associated.

need better termination checker

Wrinkle:

Backward compatibility

- Infer constraints
- New feature:
Closed type classes
- Details in paper

Open question: Forward compatibility

- Dependent types
- Termination checking
- Is Girard's paradox encodable?

Constrained type families:

- let us escape the totality trap
- prevent the usage of bogus types
- make closed type families more powerful
- simplify injective type families
- remove an unnecessary feature
- simplify the metatheory
- allow us to prove type safety



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